

Chapter 15

Investment, Time, and Capital Markets

Topics to be Discussed

- Stocks Versus Flows
- Present Discounted Value
- The Value of a Bond
- The Net Present Value Criterion for Capital Investment Decisions



Topics to be Discussed

- Adjustments for Risk
- Investment Decisions by Consumers
- Intertemporal Production Decisions---
Depletable Resources
- How are Interest Rates Determined?



Introduction

■ Capital

- Choosing an input that will contribute to output over a long period of time
- Comparing the future value to current expenditures



Stocks Versus Flows

■ Stock

- Capital is a stock measurement.
 - ◆ The amount of capital a company owns



Stocks Versus Flows

■ Flows

- Variable inputs and outputs are flow measurements.
 - ◆ An amount per time period



Present Discounted Value (PDV)

- Determining the value today of a future flow of income
 - The value of a future payment must be discounted for the time period and interest rate that could be earned.



Present Discounted Value (PDV)

■ Future Value (FV)

Future Dollar Value of \$1 invested today = $(1 + R)^n$

PDV = Present dollar value of \$1 received

in the future = $\frac{1}{(1 + R)^n}$; (how much would you have to invest today to have a dollar in the future)



Present Discounted Value (PDV)

■ Question

- What impact does R have on the PDV?



PDV of \$1 Paid in the Future

Interest Rate	1 Year	2 Years	3 Years	4 Years	5 Years	6 Years
0.01	\$0.990	\$0.980	\$0.951	\$0.905	\$0.820	\$0.742
0.02	0.980	0.961	0.906	0.820	0.673	0.552
0.03	0.971	0.943	0.863	0.744	0.554	0.412
0.04	0.962	0.925	0.822	0.676	0.456	0.308
0.05	0.952	0.907	0.784	0.614	0.377	0.231
0.06	0.943	0.890	0.747	0.558	0.312	0.174

PDV of \$1 Paid in the Future

Interest Rate	1 Year	2 Years	3 Years	4 Years	5 Years	6 Years
0.07	0.935	0.873	0.713	0.508	0.258	0.131
0.08	0.926	0.857	0.681	0.463	0.215	0.099
0.09	0.917	0.842	0.650	0.422	0.178	0.075
0.10	0.909	0.826	0.621	0.386	0.149	0.057
0.15	0.870	0.756	0.497	0.247	0.061	0.015
0.20	0.833	0.694	0.402	0.162	0.026	0.004

Present Discounted Value (PDV)

- Valuing Payment Streams
 - Choosing a payment stream depends upon the interest rate.



Two Payment Streams

	Today	1 Year	2 Years
Payment Stream A:	\$100	\$100	0
Payment Stream B:	\$20	\$100	\$100



Two Payment Streams

■ PDV of Stream $A = \frac{100}{(1+R)}$

$$\text{PDV of Stream } B = \frac{100}{(1+R)} + \frac{100}{(1+R)^2}$$



PDV of Payment Streams

$R = .05$ $R = .10$ $R = .15$ $R = .20$

PDV of Stream A: **\$195.24** **\$190.90** **\$186.96** **\$183.33**

PDV of Stream B: **205.94** **193.54** **182.57** **172.77**

Why does the PDV of A relative to B increase as R increases and vice versa for B?



The Value of Lost Earnings

- PDV can be used to determine the value of lost income from a disability or death.



The Value of Lost Earnings

■ Scenario

- Harold Jennings died in an auto accident January 1, 1986 at 53 years of age.
- Salary: \$85,000
- Retirement Age: 60



The Value of Lost Earnings

■ Question

- What is the PDV of Jennings' lost income to his family?
 - ◆ Must adjust salary for predicted increase (g)
 - Assume an 8% average increase in salary for the past 10 years



The Value of Lost Earnings

■ Question

- What is the PDV of Jennings' lost income to his family?
 - ◆ Must adjust for the true probability of death (m) from other causes
 - Derived from mortality tables



The Value of Lost Earnings

■ Question

- What is the PDV of Jennings' lost income to his family?
 - ◆ Assume $R = 9\%$
 - Rate on government bonds in 1983



The Value of Lost Earnings

$$\begin{aligned} \blacksquare \text{ PDV} &= W_0 + \frac{W_0(1+g)(1-m_1)}{(1+R)} \\ &+ \frac{W_0(1+g)^2(1-m_2)}{(1+R)^2} + \dots \\ &+ \frac{W_0(1+g)^7(1-m_7)}{(1+R)^7} \end{aligned}$$



Calculating Lost Wages

Year	$W_0(1 + g)^t$	$(1 - m_t)$	$1/(1 + R)^t$	$W_0(1 + g)^t(1 - m_t)/(1 + R)^t$
1986	\$ 85,000	.991	1.000	\$84,235
1987	91,800	.990	.917	83,339
1988	99,144	.989	.842	82,561
1989	107,076	.988	.772	81,671
1990	115,642	.987	.708	80,810
1991	124,893	.986	.650	80,043
1992	134,884	.985	.596	79,185
1993	145,675	.984	.547	78,408

The Value of Lost Earnings

■ Finding PDV

- The summation of column 4 will give the PDV of lost wages (\$650,252)
- Jennings' family could recover this amount as compensation for his death.



The Value of a Bond

- Determining the Price of a Bond
 - Coupon Payments = \$100/yr. for 10 yrs.
 - Principal Payment = \$1,000 in 10 yrs.

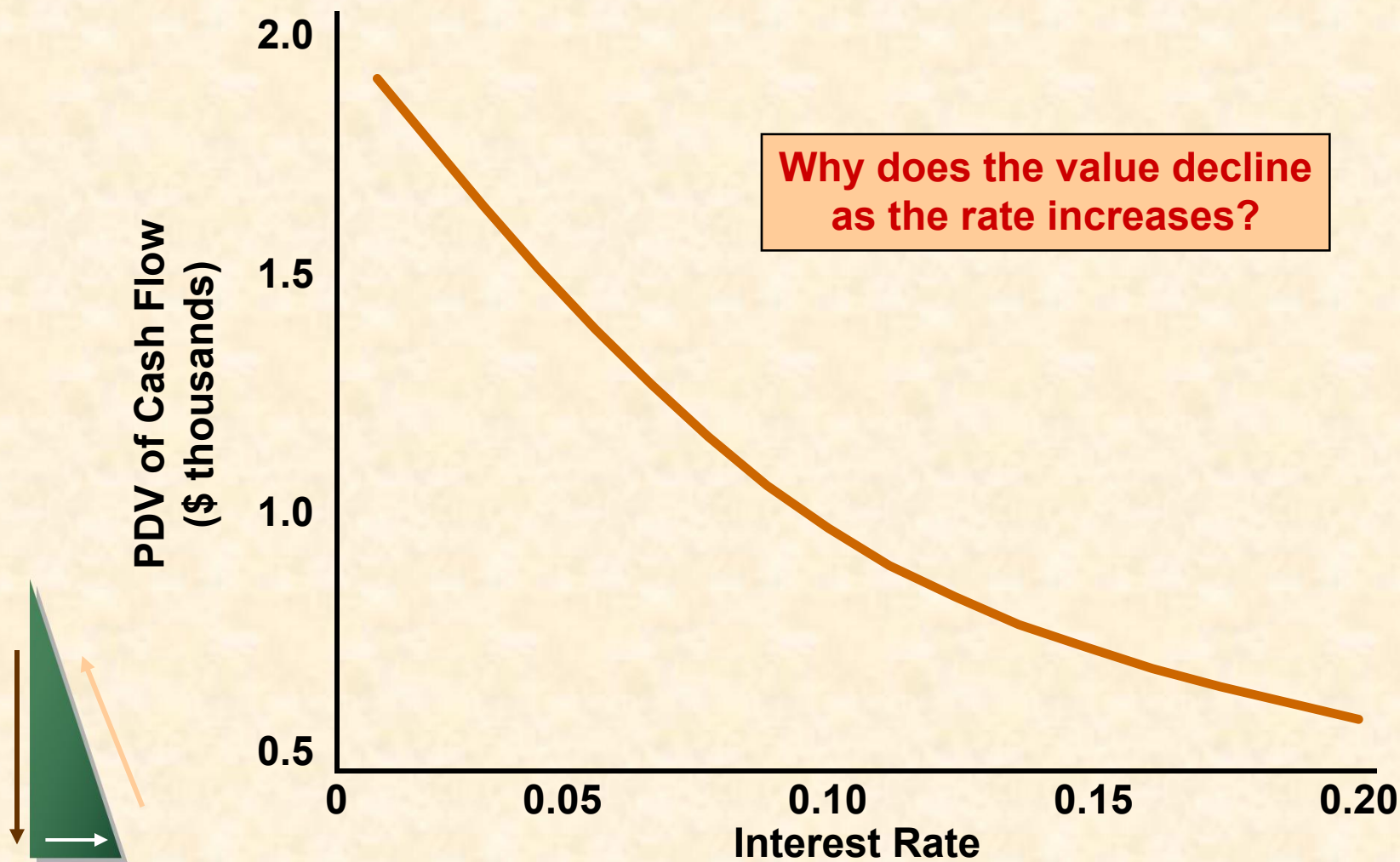
$$\begin{aligned} \text{PDV} = & \frac{\$100}{(1+R)} + \frac{\$100}{(1+R)^2} + \\ & \dots + \frac{\$100}{(1+R)^{10}} + \frac{\$1000}{(1+R)^{10}} \end{aligned}$$



Present Value of

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the Cash Flow from a Bond



The Value of a Bond

■ Perpetuities

- **Perpetuities** are bonds that pay out a fixed amount of money each year, *forever*.

$$PDV = \frac{\text{Payment}}{R}$$



Effective Yield on a Bond

- Calculating the Rate of Return From a Bond

$$P = PDV$$

$$\text{Perpetuity: } P = \frac{\text{Payment}}{R} = \frac{\$100}{R}$$

$$R = \frac{\$100}{P} \quad P = \$1,000$$

$$R = 10\%$$



Effective Yield on a Bond

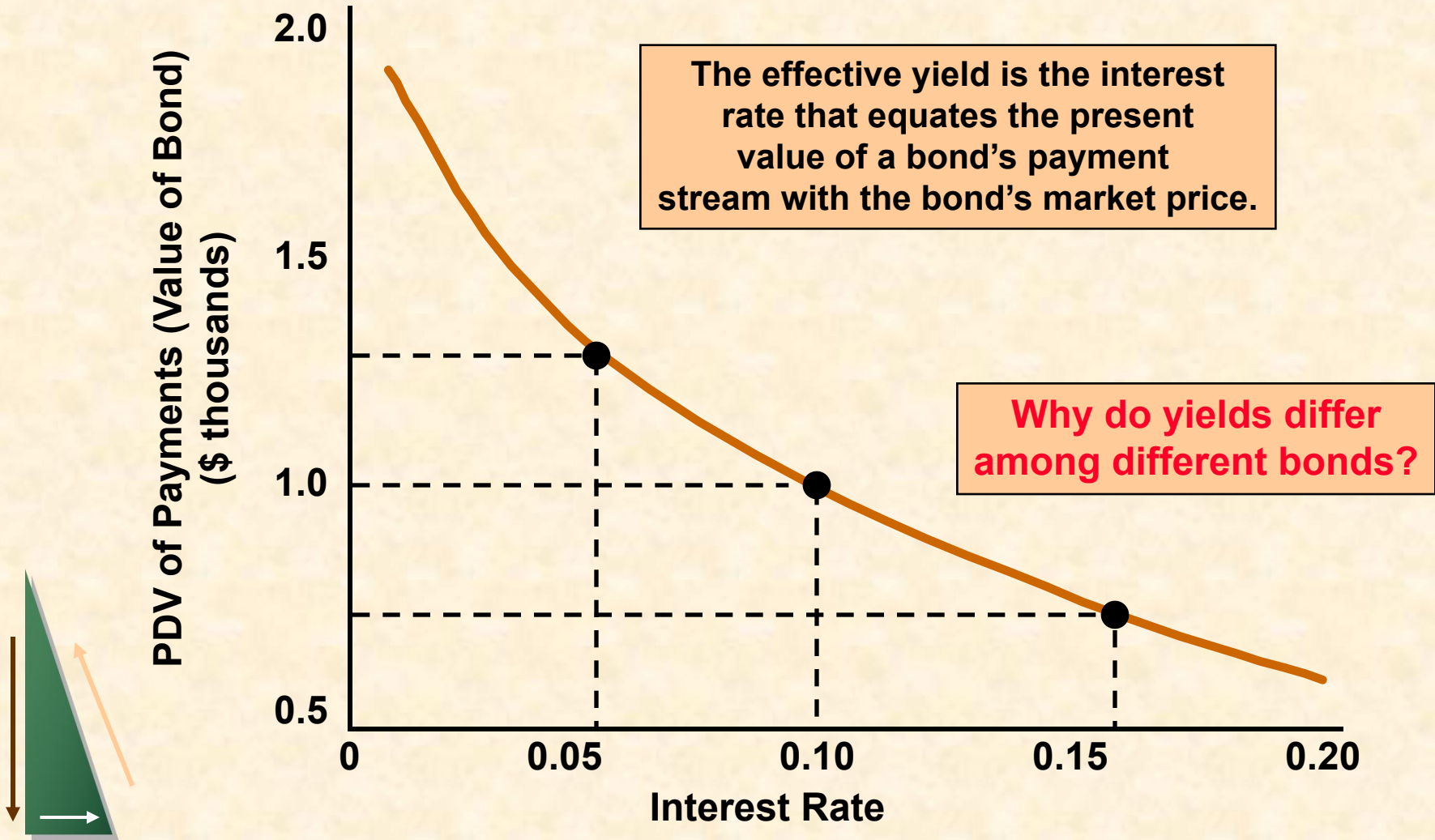
- Calculating the Rate of Return From a Bond

$$\text{Coupon Bond : PDV} = \frac{\$100}{(1+R)} + \frac{\$100}{(1+R)^2} + \dots + \frac{\$100}{(1+R)^{10}} + \frac{\$1000}{(1+R)^{10}}$$

Calculate R in terms of P



Effective Yield on a Bond



The Yields on Corporate Bonds

- In order to calculate corporate bond yields, the face value of the bond and the amount of the coupon payment must be known.

- Assume

- IBM and Polaroid both issue bonds with a face value of \$100 and make coupon payments every six months.



The Yields on Corporate Bonds

- Closing prices for each July 23, 1999:

	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>
IBM	53/8	09	5.8	30	92	-11/2
Polaroid	11 1/2	06	10.8	80	106	-5/8

a: coupon payments for one year (\$5.375)

b: maturity date of bond (2009)

c: annual coupon/closing price (\$5.375/92)

d: number traded that day (30)

e: closing price (92)

f: change in price from previous day (-1 1/2)



The Yields on Corporate Bonds

- The IBM bond yield:
 - Assume annual payments
 - 2009 - 1999 = 10 years

$$92 = \frac{5.375}{(1 + R)} + \frac{5.375}{(1 + R)^2} + \dots + \frac{5.375}{(1 + R)^{10}} + \frac{100}{(1 + R)^{10}}$$
$$R^* = 6.5\%$$



The Yields on Corporate Bonds

■ The Polaroid bond yield:

$$106 = \frac{11.5}{(1+R)} + \frac{11.5}{(1+R)^2} + \dots + \frac{11.5}{(1+R)^7} + \frac{11.50}{(1+R)^7}$$

Why was Polaroid R^* greater?



$$R^* = 10.2\%$$

The Net Present Value Criterion for Capital Investment Decisions

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- In order to decide whether a particular capital investment is worthwhile a firm should compare the present value (PV) of the cash flows from the investment to the cost of the investment.



The Net Present Value Criterion for Capital Investment Decisions

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■ NPV Criterion

- Firms should invest if the PV exceeds the cost of the investment.



The Net Present Value Criterion for Capital Investment Decisions

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■ C = capital cost

π_n = profits for n years ($n = 10$)

$$\text{NPV} = -C + \frac{\pi_1}{(1+R)} + \frac{\pi_2}{(1+R)^2} + \frac{\pi_{10}}{(1+R)^{10}}$$

R = discount rate or opportunity cost of capital
with a similar risk



Invest if $\text{NPV} > 0$

The Net Present Value Criterion for Capital Investment Decisions

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- The Electric Motor Factory (choosing to build a \$10 million factory)
 - 8,000 motors/ month for 20 yrs
 - ◆ Cost = \$42.50 each
 - ◆ Price = \$52.50
 - ◆ Profit = \$10/motor or \$80,000/month
 - ◆ Factory life is 20 years with a scrap value of \$1 million
 - Should the company invest?



The Net Present Value Criterion for Capital Investment Decisions

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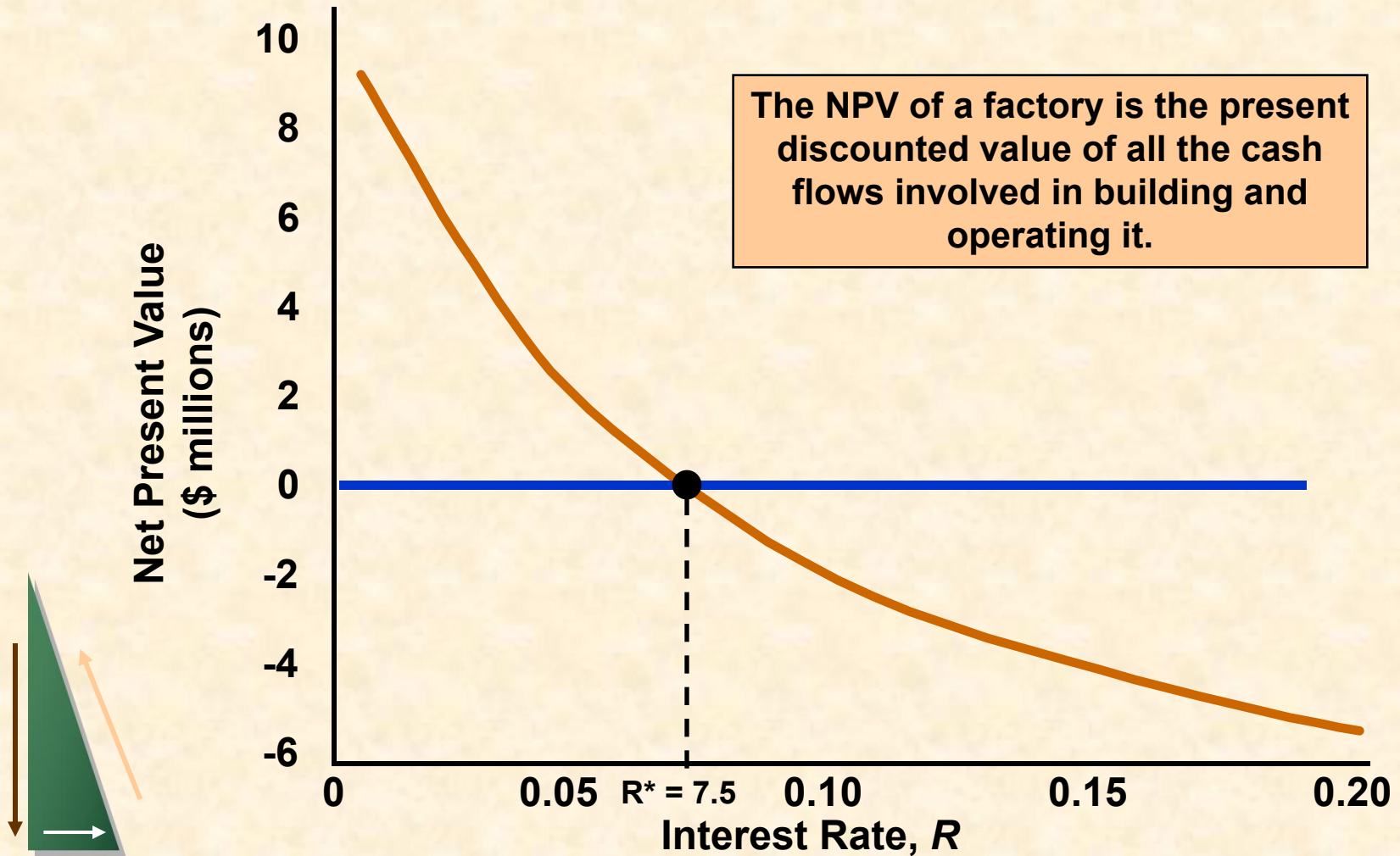
- Assume all information is certain (no risk)
 - R = government bond rate

$$\text{NPV} = -10 + \frac{.96}{(1+R)} + \frac{.96}{(1+R)^2} + \dots + \frac{.96}{(1+R)^{20}} + \frac{1}{(1+R)^{20}}$$



$$R^* = 7.5\%$$

Net Present Value of a Factory



The Net Present Value Criterion for Capital Investment Decisions

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- Real versus Nominal Discount Rates
 - Adjusting for the impact of inflation
 - Assume price, cost, and profits are in real terms
 - ◆ Inflation = 5%



The Net Present Value Criterion for Capital Investment Decisions

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- Real versus Nominal Discount Rates
 - Assume price, cost, and profits are in real terms
 - ◆ Therefore,
 - $P = (1.05)(52.50) = 55.13$, Year 2 $P = (1.05)(55.13) = 57.88\dots$
 - $C = (1.05)(42.50) = 44.63$, Year 2 $C = \dots$
 - Profit remains \$960,000/year



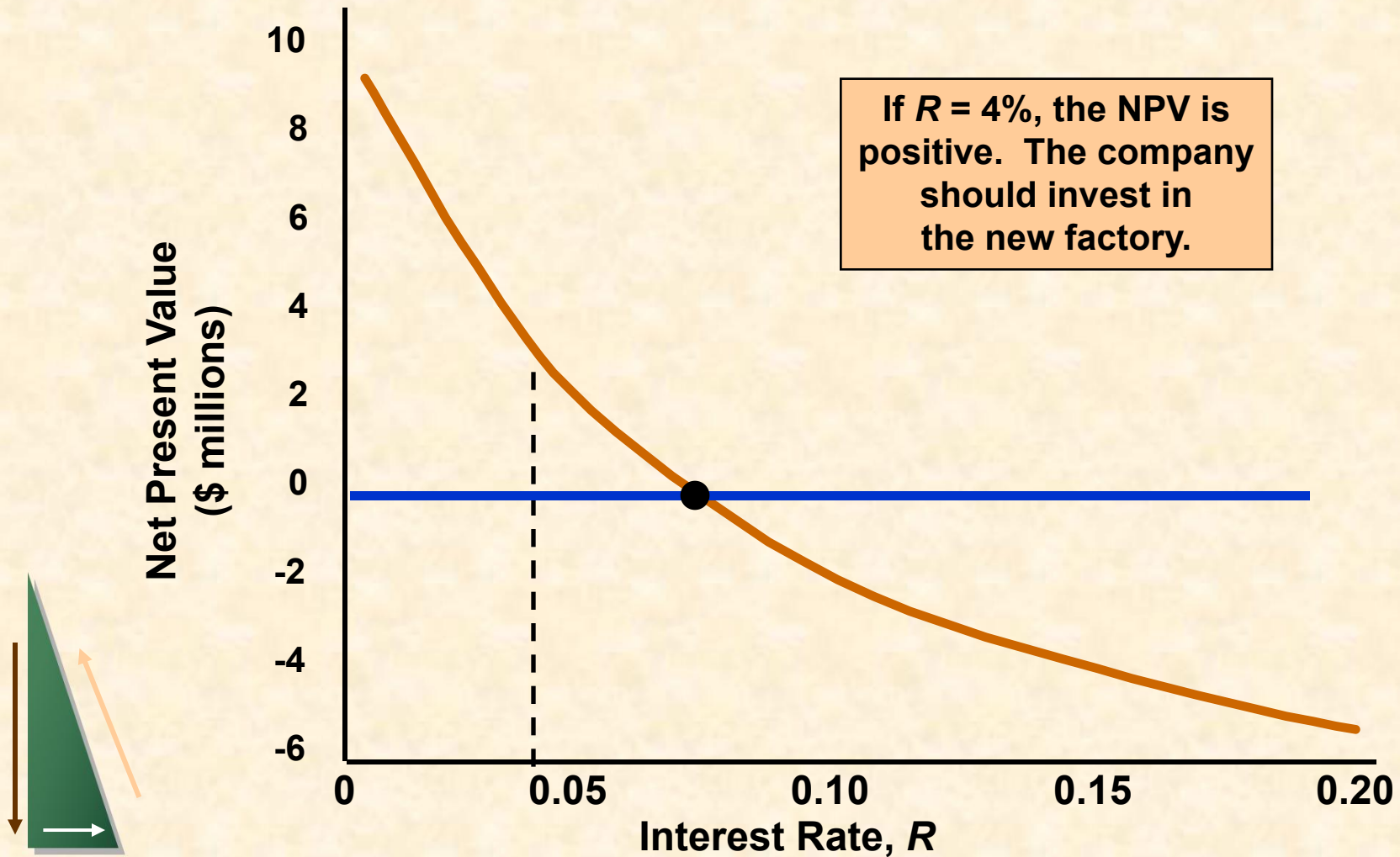
The Net Present Value Criterion for Capital Investment Decisions

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- Real versus Nominal Discount Rates
 - Real $R = \textit{nominal } R - \textit{inflation} = 9 - 5 = 4$



Net Present Value of a Factory



The Net Present Value Criterion for Capital Investment Decisions

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- Negative Future Cash Flows
 - Investment should be adjusted for construction time and losses.



The Net Present Value Criterion for Capital Investment Decisions

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- Electric Motor Factory
 - Construction time is 1 year
 - ◆ \$5 million expenditure today
 - ◆ \$5 million expenditure next year
 - Expected to lose \$1 million the first year and \$0.5 million the second year
 - Profit is \$0.96 million/yr. until year 20
 - Scrap value is \$1 million



The Net Present Value Criterion for Capital Investment Decisions

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$$\begin{aligned} \blacksquare \text{ NPV} = & -5 - \frac{5}{(1+R)} - \frac{1}{(1+R)^2} - \frac{.5}{(1+R)^3} \\ & + \frac{.96}{(1+R)^4} + \frac{.96}{(1+R)^5} + \dots \\ & + \frac{.96}{(1+R)^{20}} + \frac{1}{(1+R)^{20}} \end{aligned}$$



Adjustments for Risk

- Determining the discount rate for an uncertain environment:
 - This can be done by increasing the discount rate by adding a *risk-premium* to the risk-free rate.
 - ◆ Owners are risk averse, thus risky future cash flows are worth less than those that are certain.



Adjustments for Risk

- Diversifiable Versus Nondiversifiable Risk
 - **Diversifiable risk** can be eliminated by investing in many projects or by holding the stocks of many companies.
 - **Nondiversifiable risk** cannot be eliminated and should be entered into the risk premium.



Adjustments for Risk

- Measuring the Nondiversifiable Risk Using the Capital Asset Pricing Model (CAPM)
 - Suppose you invest in the entire stock market (mutual fund)
 - ◆ r_m = expected return of the stock market
 - ◆ r_f = risk free rate
 - ◆ $r_m - r_f$ = risk premium for nondiversifiable risk



Adjustments for Risk

- Measuring the Nondiversifiable Risk Using the Capital Asset Pricing Model (CAPM)

- Calculating Risk Premium for One Stock

$$r_1 - r_f = \beta(r_m - r_f)$$

r_1 = expected return

β = asset beta = measures the sensitivity

of the asset's return to market movements



Adjustments for Risk

■ Question

- What is the relationship between the nondiversifiable risk and the value of the *asset beta*?



Adjustments for Risk

- Given beta, we can determine the correct discount rate to use in computing an asset's net present value:

$$\text{Discount Rate} = r_f + \beta(r_m - r_f)$$



Adjustments for Risk

- Determining beta
 - Stock
 - ◆ Estimated statistically for each company



Adjustments for Risk

■ Determining beta

● Factory

- ◆ Weighted average of expected return on the company's stock and the interest on the debt
 - Expected return depends on beta
- ◆ *Caution:* The investment should be typical for the company



Investment Decisions by Consumers

- Consumers face similar investment decisions when they purchase a durable good.
 - Compare *future* benefits with the *current* purchase cost



Investment Decisions by Consumers

- Benefits and Cost of Buying a Car
 - S = value of transportation services in dollars
 - E = total operating cost/yr
 - Price of car is \$20,000
 - Resale value of car is \$4,000 in 6 years



Investment Decisions by Consumers

■ Benefits and Cost

$$NPV = -20,000 + (S - E) + \frac{(S - E)}{(1 + R)}$$

$$\frac{(S - E)}{(1 + R)^2} + \dots + \frac{(S - E)}{(1 + R)^6} + \frac{4000}{(1 + R)^6}$$



Choosing an Air Conditioner

- Buying a new air conditioner involves making a trade-off.
 - Air Conditioner A
 - ◆ Low price and less efficient (high operating cost)



Choosing an Air Conditioner

- Buying a new air conditioner involves making a trade-off.
 - Air Conditioner *B*
 - ◆ High price and more efficient
 - Both have the same cooling power
 - Assume an 8 year life



Choosing an Air Conditioner

■
$$PDV = C_i + OC_i + \frac{OC_i}{(1+R)} +$$

$$\frac{OC_i}{(1+R)^2} + \dots + \frac{OC_i}{(1+R)^8}$$

C_i is the purchase price of i

OC_i is the average operating cost of i



Choosing an Air Conditioner

- Should you choose *A* or *B*?
 - Depends on the discount rate
 - ◆ If you borrow, the discount rate would be high
 - Probably choose a less expensive and inefficient unit
 - ◆ If you have plentiful cash, the discount rate would be low.
 - Probably choose the more expensive unit



Intertemporal Production

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Decisions---Depletable Resources

- Firms' production decisions often have *intertemporal* aspects---production today affects sales or costs in the future.



Intertemporal Production

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Decisions---Depletable Resources

■ Scenario

- You are given an oil well containing 1000 barrels of oil.
- MC and $AC = \$10/\text{barrel}$
- Should you produce the oil or save it?



Intertemporal Production

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Decisions---Depletable Resources

■ Scenario

- P_t = price of oil this year
- P_{t+1} = price of oil next year
- C = extraction costs
- R = interest rate

■ If $(P_{t+1} - c) > (1 + R)(P_t - c)$: Keep the oil in the ground

If $(P_{t+1} - c) < (1 + R)(P_t - c)$: Sell all the oil now

If $(P_{t+1} - c) = (1 + R)(P_t - c)$: Indifferent



Intertemporal Production

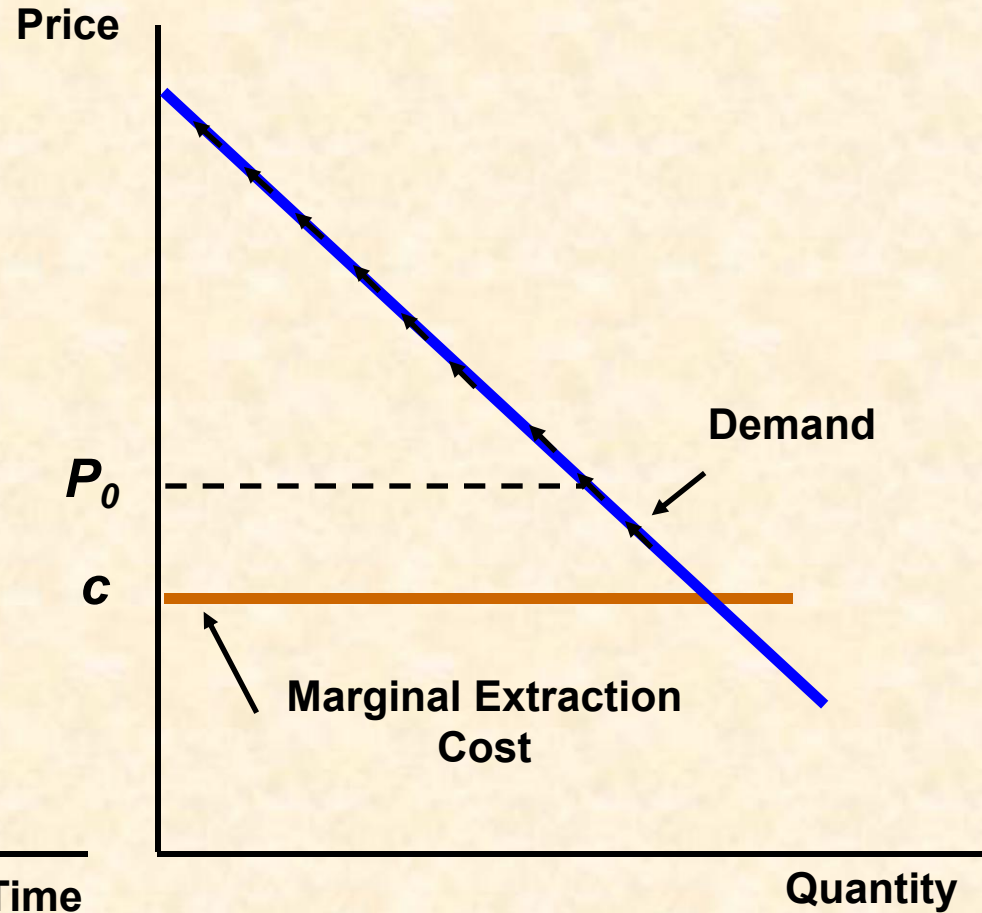
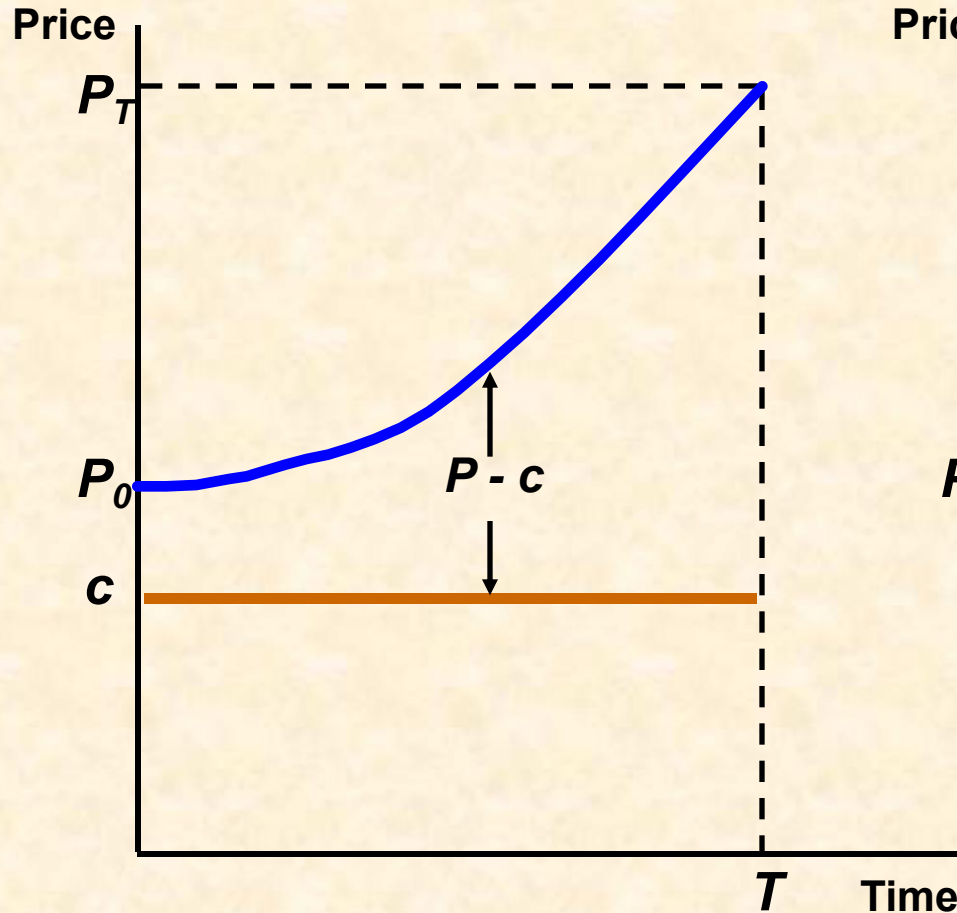
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Decisions---Depletable Resources

- Do not produce if you expect its price less its extraction cost to rise faster than the rate of interest.
- Extract and sell all of it if you expect price less cost to rise at less than the rate of interest.
- What will happen to the price of oil?



Price of an Exhaustible Resource



Price of an Exhaustible Resource

- In a competitive market, $Price - MC$ must rise at exactly the rate of interest.
- Why?
 - How would producers react if:
 - ◆ $P - C$ increases faster than R ?
 - ◆ $P - C$ increases slower than R ?



Price of an Exhaustible Resource

■ Notice

- $P > MC$

- ◆ Is this a contradiction to the competitive rule that $P = MC$?

- *Hint:* What happens to the opportunity cost of producing an exhaustible resource?



Price of an Exhaustible Resource

■ $P = MC$

- $MC = \text{extraction cost} + \text{user cost}$
- $\text{User cost} = P - \text{marginal extraction cost}$



Price of an Exhaustible Resource

- How would a monopolist choose their rate of production?
 - They will produce so that marginal revenue revenue less marginal cost rises at exactly the rate of interest, or
 - $(MR_{t+1} - c) = (1 + R)(MR_t - c)$



Price of an Exhaustible Resource

Resource Production by a Monopolist

- The monopolist is *more conservationist* than a competitive industry.
 - They start out charging a higher price and deplete the resources more slowly.



How Depletable Are

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Depletable Resources?

Resource User Cost/Competitive Price

Crude oil	.4 to .5
Natural gas	.4 to .5
Uranium	.1 to .2
Copper	.2 to .3
Bauxite	.05 to .2
Nickel	.1 to .2
Iron Ore	.1 to .2
Gold	.05 to .1



How Depletable Are

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Depletable Resources?

- The market structure and changes in market demand have had a very dramatic impact on resource prices over the past few decades.

- **Question**

- Why would oil and natural gas have such a high user cost ratio compared to the other resources?



How Are Interest Rates Determined?

- The interest rate is the price that borrowers pay lenders to use their funds.
 - Determined by supply and demand for loanable funds.

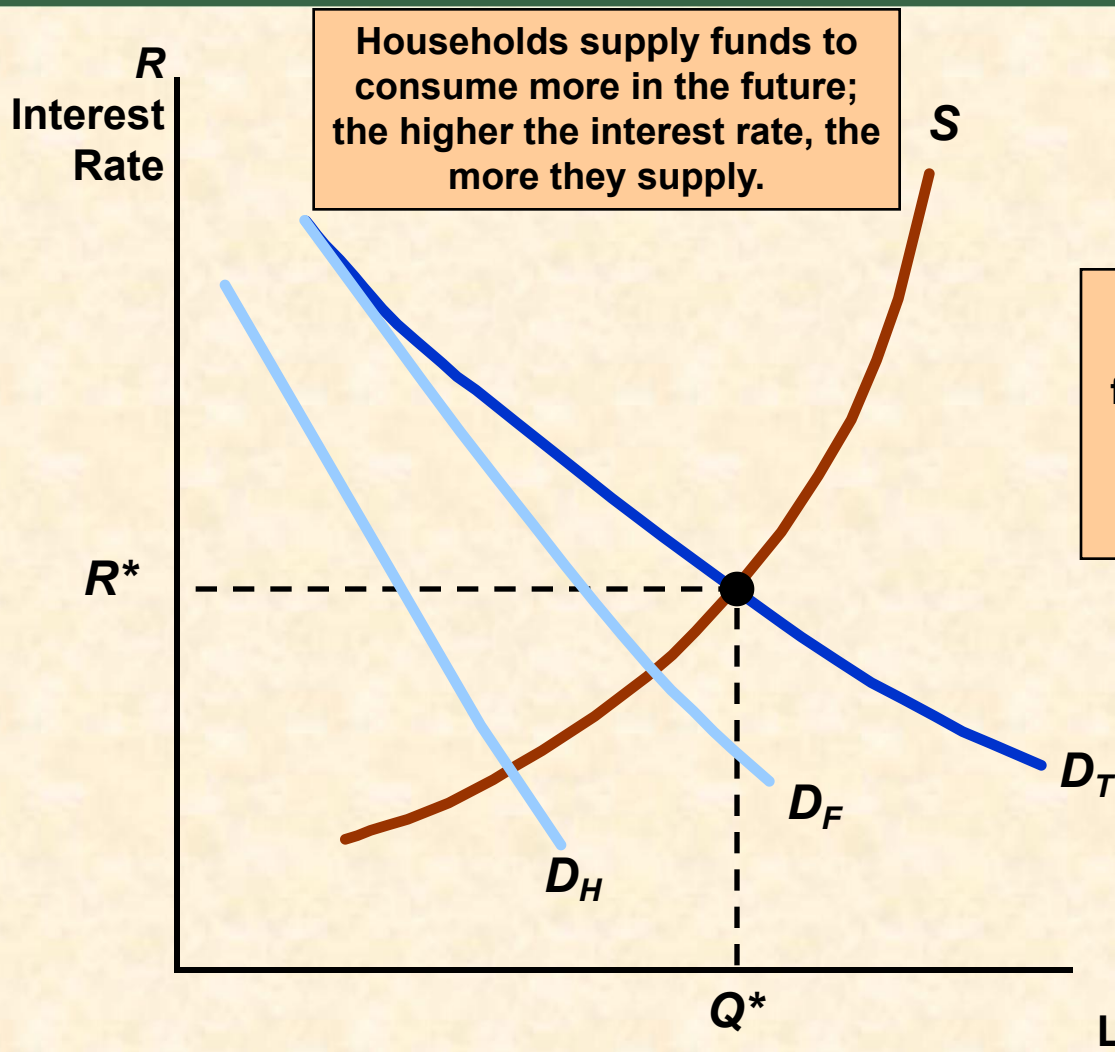


Supply and Demand for Loanable Funds

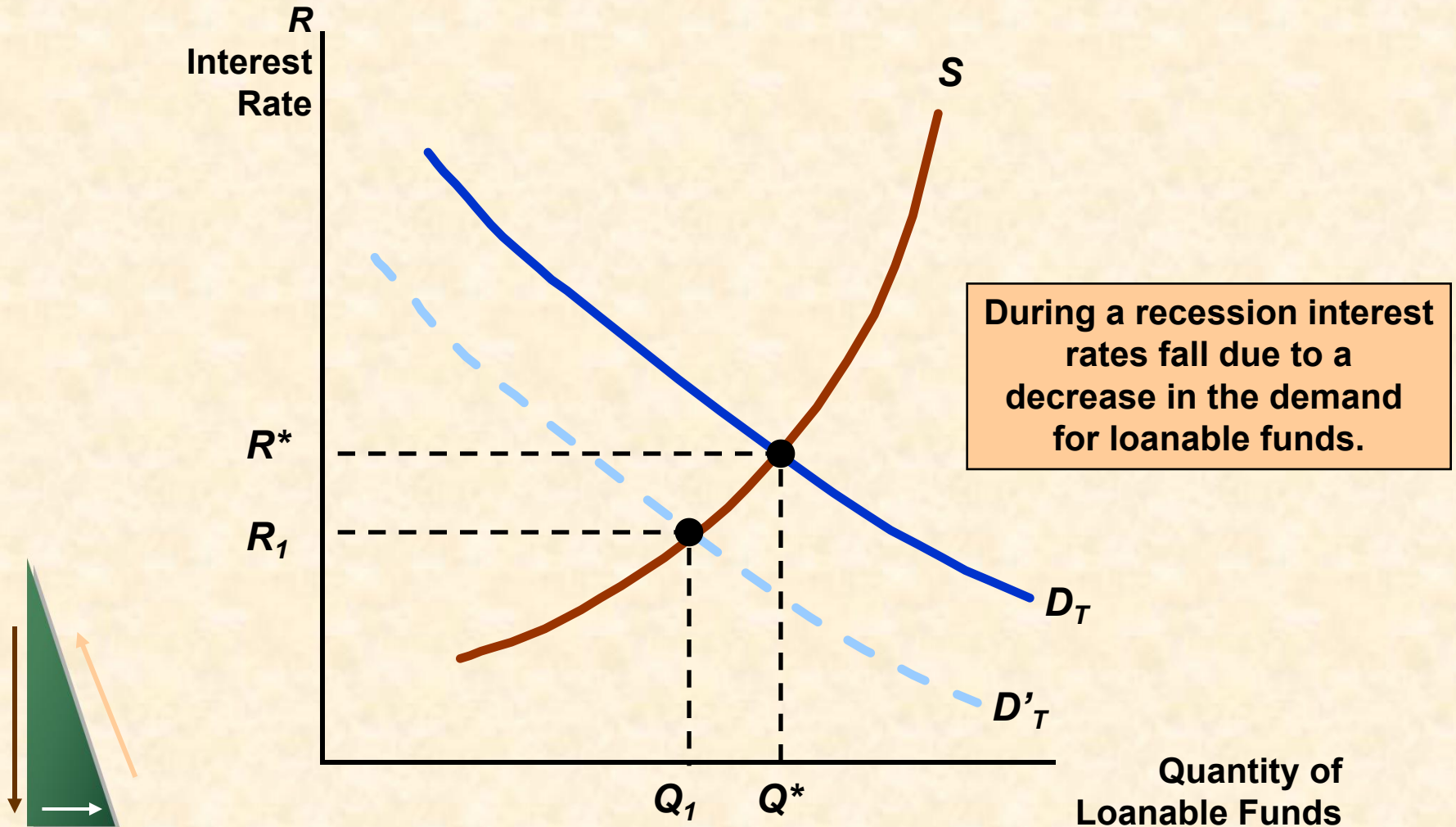
Households supply funds to consume more in the future; the higher the interest rate, the more they supply.

D_H and D_F , the quantity demanded for loanable funds by households (H) and firms, respectively, varies inversely with the interest rate.

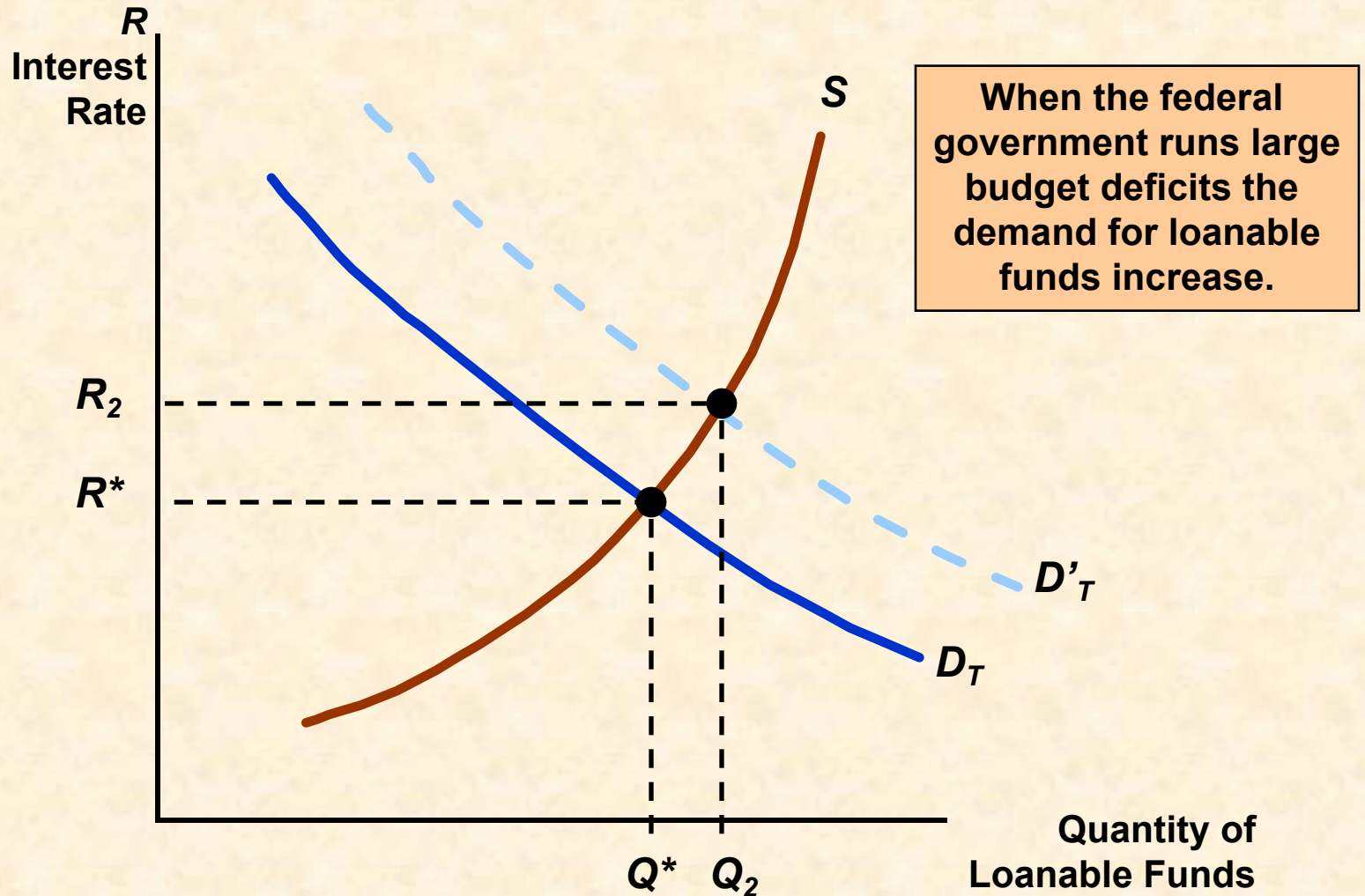
$D_T = D_H + D_F$ and equilibrium interest rate is R^* .



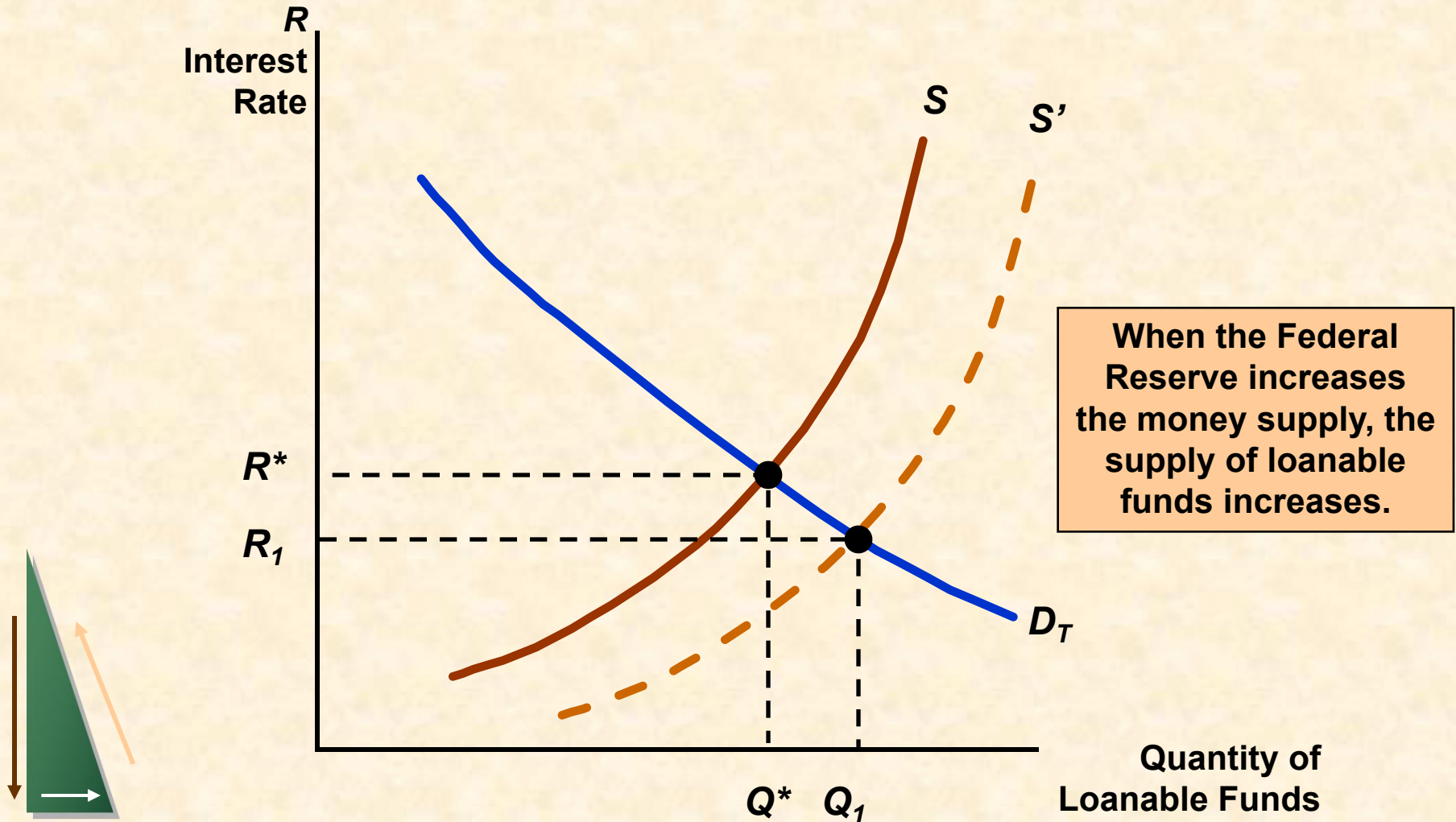
Changes In The Equilibrium



Changes In The Equilibrium



Changes In The Equilibrium



How Are Interest Rates Determined?

■ A Variety of Interest Rates

- 1) Treasury Bill Rate
- 2) Treasury Bond Rate
- 3) Discount Rate



How Are Interest Rates Determined?

- A Variety of Interest Rates
 - 4) Commercial Paper Rate
 - 5) Prime Rate
 - 6) Corporate Bond Rate



Summary

- A firm's holding of capital is measured as a stock, but inputs of labor and raw materials are flows.
- When a firm makes a capital investment, it spends money now, so that it can earn profits in the future.



Summary

- The present discounted value (PDV) of \$1 paid n years from now is $\$1/(1 + R)^n$.
- A bond is a contract in which a lender agrees to pay the bondholder a stream of money.



Summary

- Firms can decide whether to undertake a capital investment by applying the NPV criterion.
- The discount rate that a firm uses to calculate the NPV for an investment should be the opportunity cost of capital.



Summary

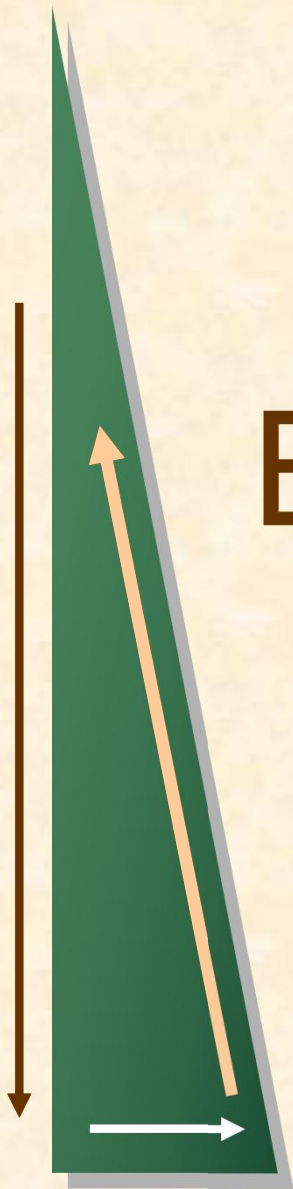
- An adjustment for risk can be made by adding a risk premium to the discount rate.
- Consumers are also faced with investment decisions that require the same kind of analysis as those of firms.



Summary

- An exhaustible resource in the ground is like money in the bank and must earn a comparable return.
- Market interest rates are determined by the demand and supply of loanable funds.





End of Chapter 15

Investment, Time, and Capital Markets